



Minifrac Analysis: A Comprehensive Overview



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0.2 Minifrac Definition



- Minifrac tests consist of injecting a small volume of fluid into a target formation at a defined rate to create fracture(s).
- The fracture(s) are allowed to close, while the pressure is monitored and recorded.
- **Objective:** To obtain distinct and useful information from analyses of the various test intervals, while minimizing cost, time, and formation damage.



0.3 Minifrac vs. DFIT



- **Minifrac (MF) Tests have various other names:**
 - Fracture Diagnostic Tests (FDT)
 - Fracture Calibration Tests (FCT)
 - Diagnostic Fracture Injection Tests (DFIT®) (trademark of Halliburton)
- **Proposed Distinction**
 - Minifrac for Conventional sandstone reservoirs (that flow without frac)
Rate same as the Mainfrac. X-linked fluid (usually same as Mainfrac).
 - DFIT for Unconventional shale reservoirs (that do not flow without frac)
Rate much lower than Mainfrac. Newtonian or Linear fluid (may be different for Mainfrac).



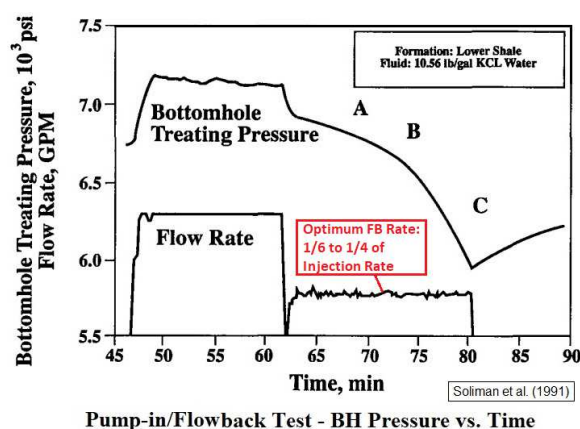
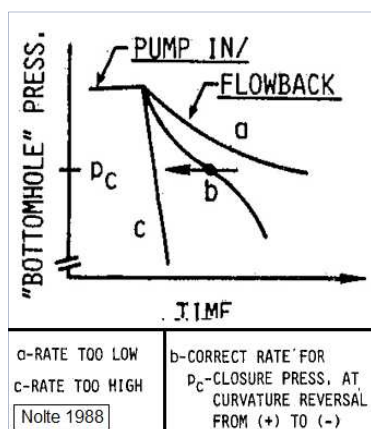
0.4 Intro: Types of Minifrac Tests



- Pump-in / Flow-back
 - Not performed very often (usually no flow-back meter rigged-up)
- Equilibrium Test
 - Not performed very often.
- Pump-in / Shut-in
 - Performed routinely (is being discussed extensively).
- Leak-Off Test (LOT) and Extended Leak-off Test (ELOT)
 - Both are performed during drilling (Not covered)

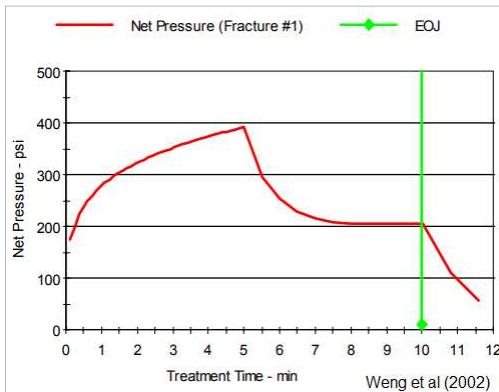
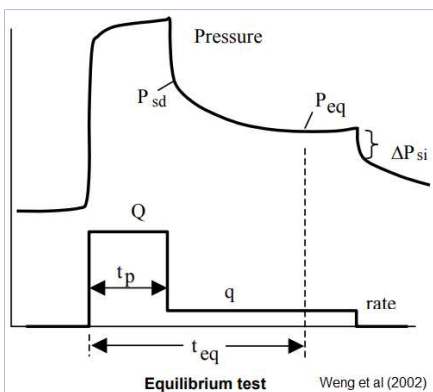


0.5 Pump-in Flowback



Difficult to determine the correct flowback rate

0.6 Equilibrium Test



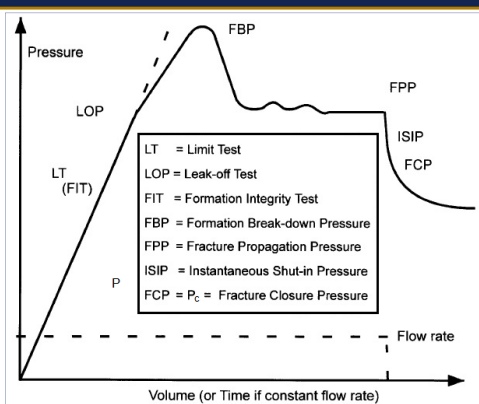
Normal injection rate (Q) is followed by very low rate (q) until a stabilized equilibrium pressure is reached, and the pressure starts to increase.

P_{eq} is an upper bound for P_c

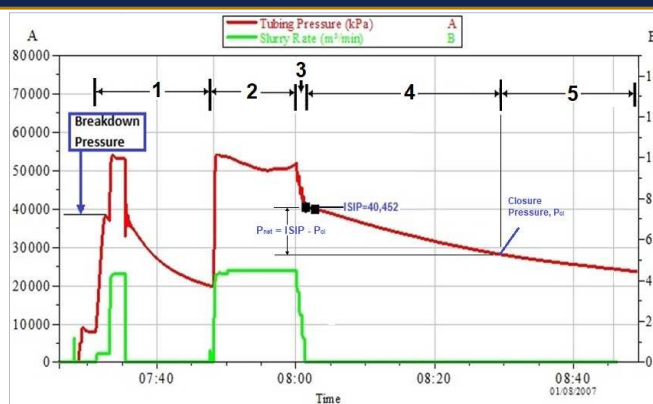
Poulsen (1996)
Weng et al. (2002)



0.7 Microfrac vs. Minifrac



Microfrac (Gals/min)



Minifrac (Bbls/min or m³/min)

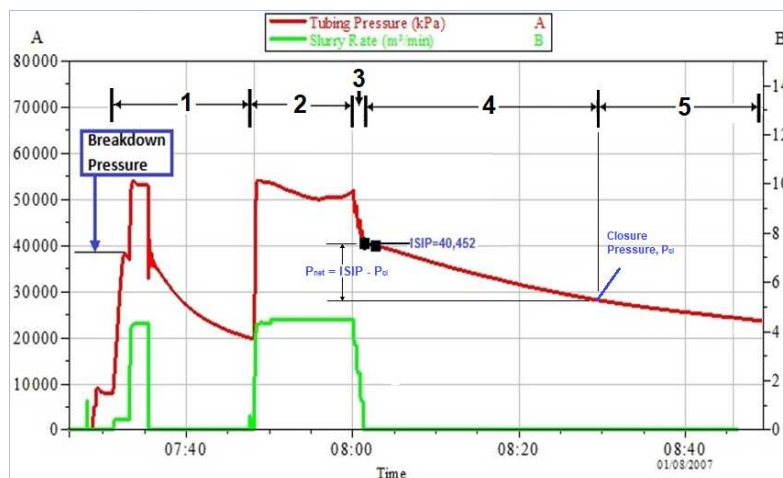
Formation break happens at very low injection rate



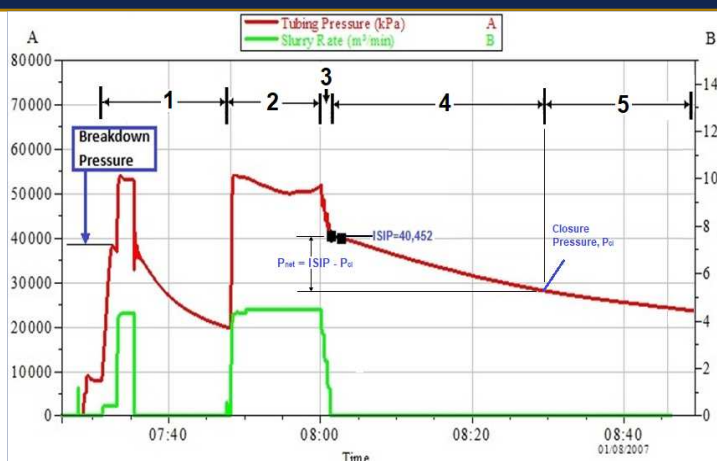
0.8 Test Events and Analyses



- 1 Formation Breakdown (FBD)
- 2 Minifrac Injection
- 3 Rate Step-down Test (RST)
- 4 Before Closure Analysis (BCA)
- 5 After Closure Analysis (ACA)



1.0 Formation Breakdown (FBD)



- **Formation Breakdown (FBD) consists of two intervals:**
 - **Injection**
 - **Shut-in**
 - **Theory:**
 - **Injection volume should be small and with clean linear (Newtonian) fluids in order to observe the baseline behavior of the formation.**
- Note that the rate required to initiate fracturing is very low**

1.1 FBD Procedure



■ Procedure:

1. Fill well and start Injecting WB fluid at very low rate (0.15-0.25 bpm).
2. Continue by increasing injection rate by small increments (0.15-0.25 bpm) until an **abrupt** pressure reduction is noted. The highest pressure reached is the formation breakdown pressure.
3. Divide by TVD to obtain the frac gradient.
4. Increase injection rate to that of the main treatment rate and inject the remaining fluid volume that has been scheduled for the FBD. Volume depends on the type of formation and the permeability.
5. Shut-in for 15-30 min.
6. Monitor and record pressure.



1.2 Formation Break not Clear



Loc.: Arabian Peninsula
Depth: 4600 m
K: 0.05 mD
 ϕ : 0.07 %
Temp: 280 °C
H: 15 m



If not clear break noted, Use stabilized pressure as formation break pressure or ISIP

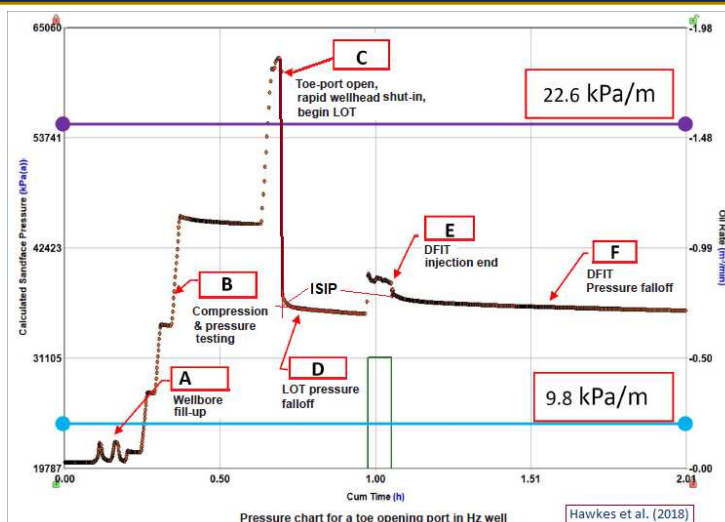
1.3 Formation Break: Toe & Sliding Sleeves



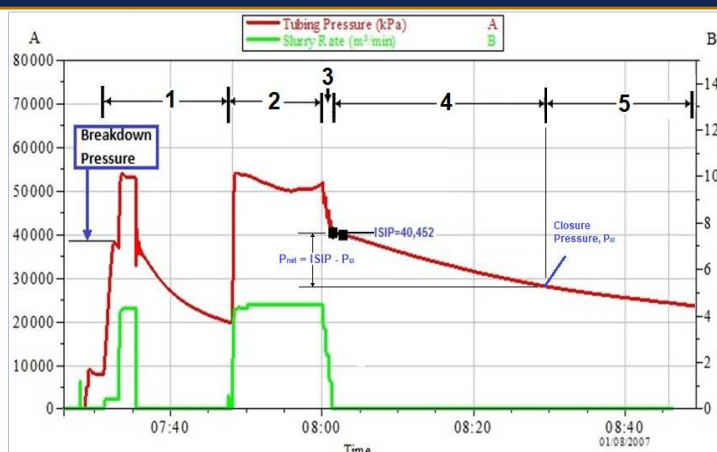
When pressuring up to open a Toe sleeve or a Sliding sleeve, the correct formation break pressure isn't recorded.

In such cases, use the ISIP to calculate the Fracture Gradient.

$$FG = ISIP / TVD$$



2.0 Minifrac

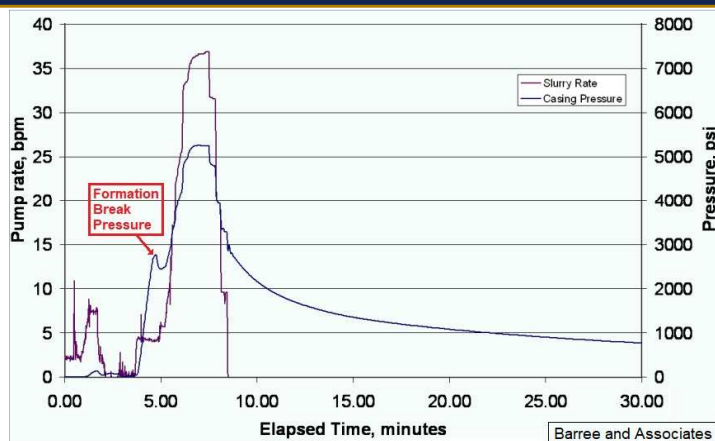


1. Inject X-linked gel fluid. Rate must be equal to that of mainfrac.
2. Overdisplace with linear fluid (Slickwater - visc-10 cp).
3. Perform RST at end of Minifrac.

Considerations:

- Wellbore volume
- Friction in: Wellbore, Perforations and Near-wellbore.
- Formation Permeability
- Formation Thickness

2.1 Diagnostic Fracture Injection Test (DFIT)



1. Inject clear Newtonian fluid (Usually WB Fluid).
Rate may be lower than mainfrac.
Low rate to Formation break.
2. Perform RST at end of DFIT.
3. No need to displace.

Considerations:

- Formation Permeability
- Formation Thickness
- Friction in: Wellbore, Perforation, Near-wellbore.

2.2 General DFIT Design Rules for Unconventional formations



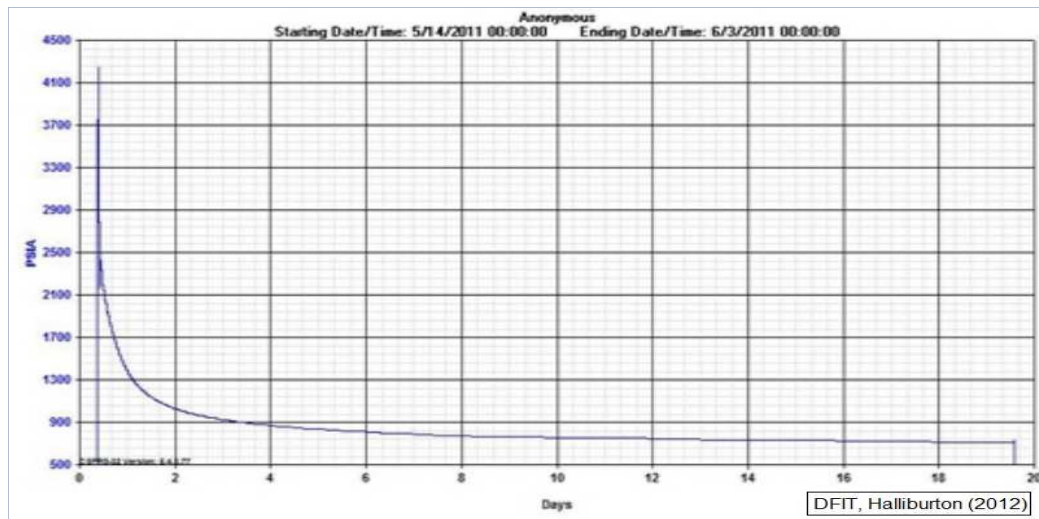
- Injection Volume (typical): 1 to 60 bbls
- Injection Rate (Typical): 0.1 to 15 bbls/min.
- Type of fluid: Clear Newtonian (2-3 % KCl water)

Injection Period (min)	Permeability (md)	Time to Closure Pressure
5	0.1	0.2 hr (12 min)
20	0.1	10 hr
5	0.01	2-3 days
5	0.0001	10 days



JPT, Sept 2014

2.3 DFIT Example



2.4 Minifrac Design Volume for RST



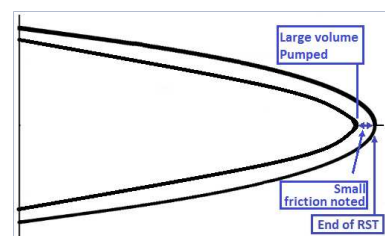
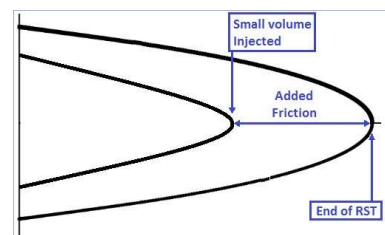
Fluid Volume:

Theory:

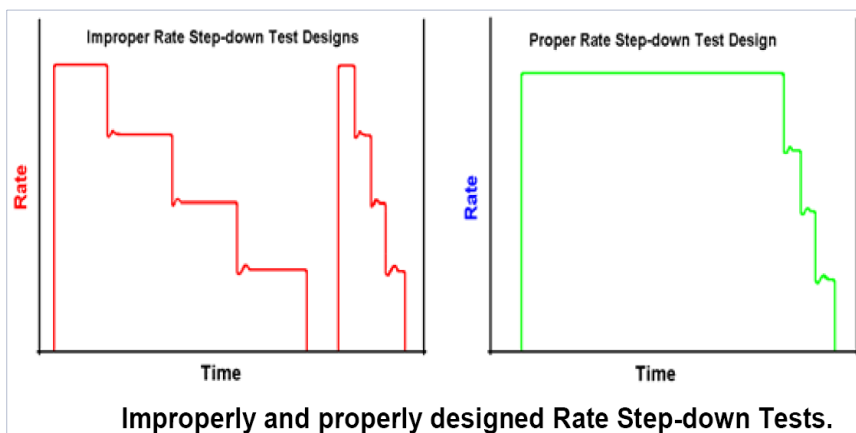
In order to prepare for the RST at the end of the Minifrac, The fluid volume injected should be fairly large, such that during the very small interval of the RST (30-45 sec), the increase in fracture size isn't very large. (See fracture profiles).

Reason:

The friction in the fracture will not change during the extremely short interval of the RST.



2.5 Minifrac Design for RST



Proper and Improper designs of RST are shown.

Substantial amount of fluid must be injected prior to performing the RST.

The steps must be very short (10-15 sec) and rapid.

Massaras et al. 2007

2.6 Rate to Initiate Fracturing Equation



$$q_{i,max} = \frac{4.917 \times 10^{-6} kh[(FG * D) - \Delta p_{safe} - p]}{\mu \beta (\ln \frac{r_e}{r_w} + s)}$$

Where,	$q_{i,max}$	=	injection rate in bbl/min
	k	=	permeability of undamaged formation, md
	h	=	net thickness, ft
	FG	=	fracture gradient, psi/ft
	D	=	depth, ft
	Δp_{safe}	=	safety margin, psi
	p	=	reservoir pressure, psi
	μ	=	viscosity of injected fluid, cp
	β	=	formation volume factor
	r_e	=	drainage radius, ft
	r_w	=	wellbore radius, ft
	s	=	skin



For **low to moderate** permeability, an injection rate of **1-2 bpm** can initiate and propagate hydraulic fracturing.

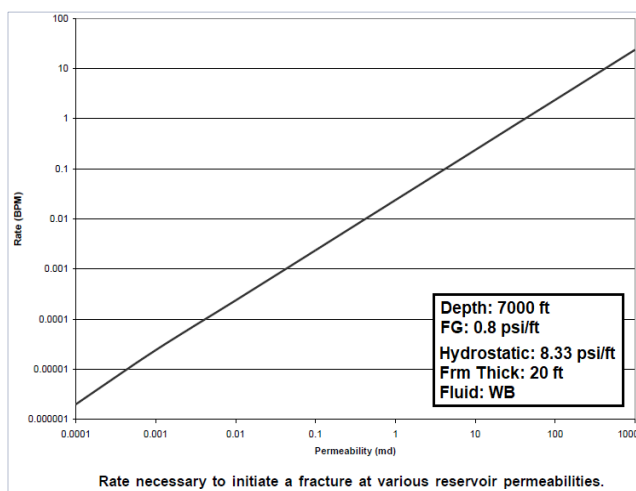
For **micro- and nano-Darcy** the rate is **lower**. It can be estimated by using the plot of the next slide.

For specific situations, approximate injection rates can be estimated with Darcy's Radial Flow equation (left).

Generally, to propagate a fracture, the injection rate must be high enough so that the treating pressure exceeds the Fracture Extension Pressure (**FEP**).

Barree et al. 2014

2.7 Rate to Initiate Fracturing Plot



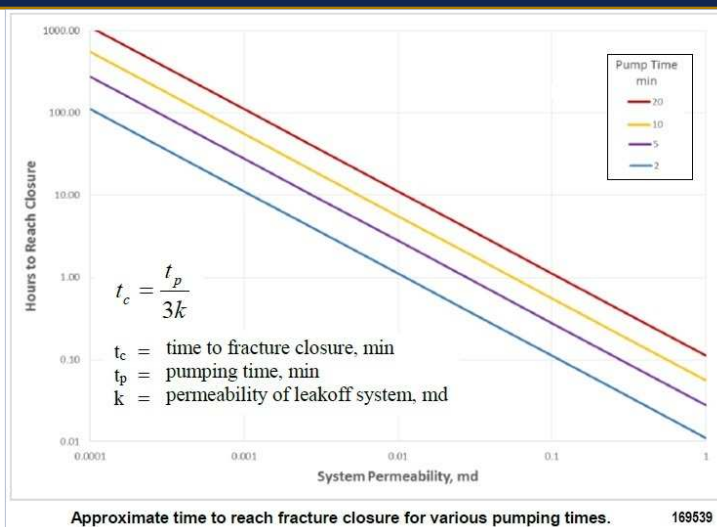
Use equation (previous slide) or the plot to estimate rate to initiate fracturing.

After fracture initiation, a maximum injection rate of 5-6 bpm or 7-8 bpm is adequate.

For injecting 3-5 minutes,
The max volumes would be:
Min: $3 \times 6 = 18$ bbls
Max: $5 \times 8 = 40$ bbls

Barree et al. (2014)

2.8 Time to Closure

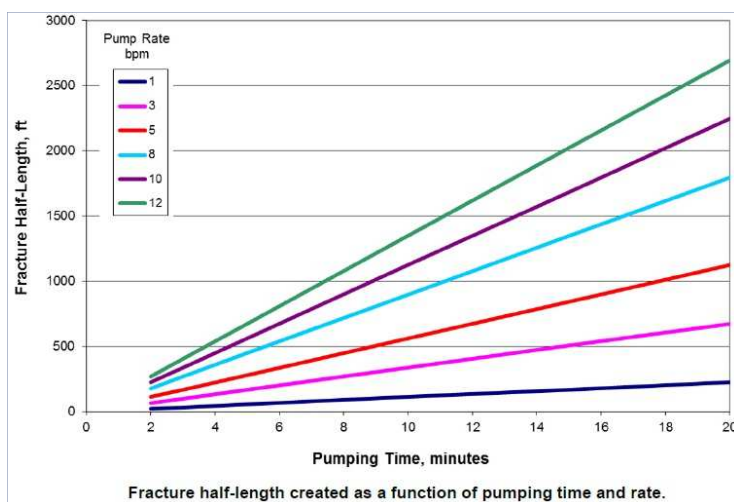


Estimated time to closure for pumping times of 2 to 20 min.

For longer pump times, use the equation.

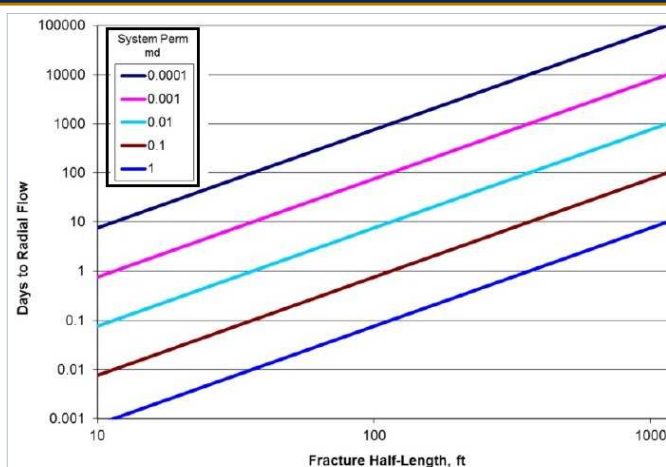
Barree et al. 2014

2.9 Frac Length Created



Barree et al. (2014)

2.10 Time to Pseudoradial



$$t_{pr} = \frac{\phi \mu C_f x_f^2 t_{Dxf}}{0.0002637k}$$

t_{pr} = time to reach pseudo-radial flow, hours
 ϕ = porosity, fraction
 μ = fluid viscosity, cp
 C_t = total reservoir compressibility, 1/psi
 x_f = fracture half-length, ft
 k = permeability of leakoff system, md

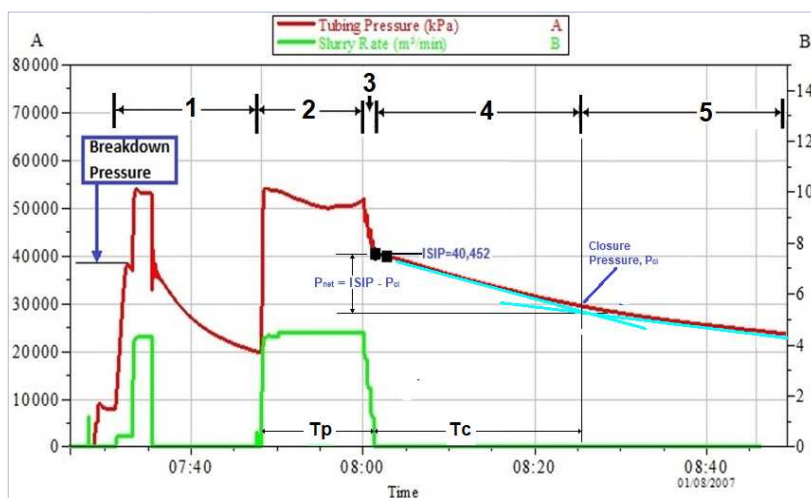
$t_{Dxf}=1$ for a gas reservoir
 viscosity of 0.02 cp,
 porosity of 8%,
 fracture height of 30 feet
 total reservoir
 compressibility of 3.0e-5/psi.

Barree et al., 2014

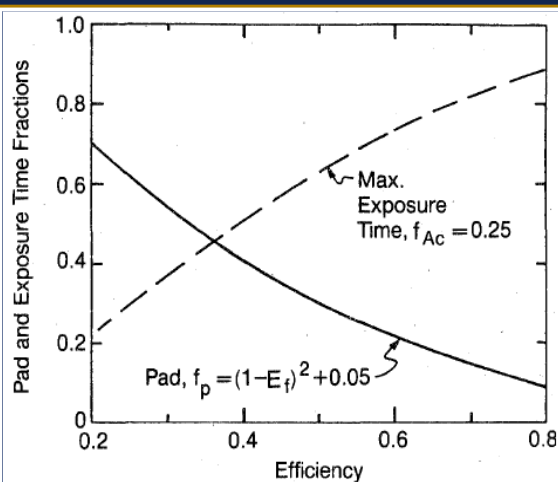
2.11 Results from Basic Minifrac Analyses



- Breakdown Pressure (P_{br})
- Instantaneous Shut-in Pressure (ISIP)
- Closure Pressure (P_{cl})
- Net-pressure ($P_{net} = ISIP - P_{cl}$)
- Pumping Time (T_p)
- Closure Time (T_c)
- Fluid / Fracture (F.E., E_f)
- Pad Percentage (%)
- Pad Size (Vol)



2.12 Nolte Fluid Efficiency-Pad Equations



Pad and exposure relations with efficiency.

$$F.E. - E_f = \frac{\left(1 + \frac{T_c}{T_p}\right)^{1.5} - \left(\frac{T_c}{T_p}\right)^{1.5}}{\left(1 + \frac{T_c}{T_p}\right)^{1.5} - \left(\frac{T_c}{T_p}\right)^{1.5}} - 1$$

Nolte Method:

$$\% \text{ Pad Volume} = (1 - F.E.)^2 + 0.05$$

Kane Method (HAL):

$$\% \text{ Pad Volume} = (1 - F.E.)^2$$

Shell Method % (Pad + Prepad):

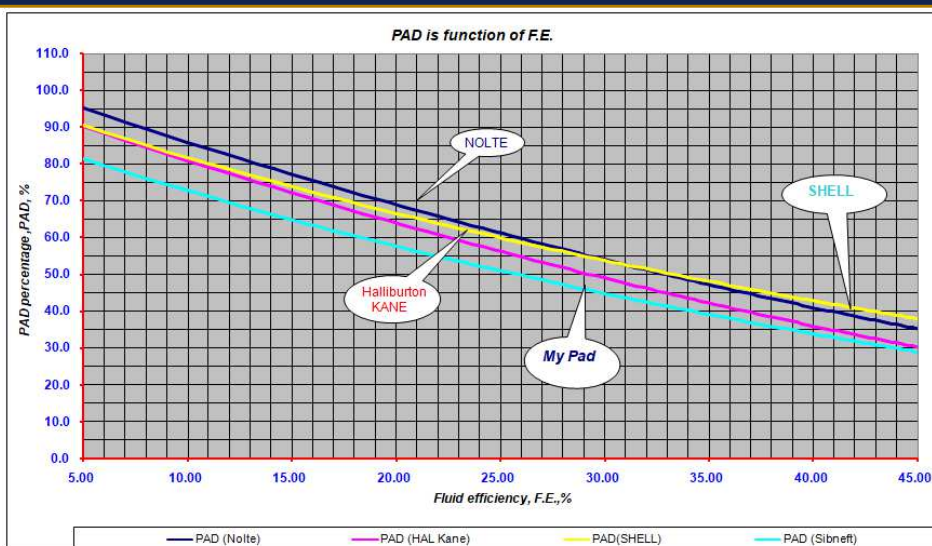
$$\% (\text{Pad} + \text{Prepad}) = (1 - F.E.) / (1 + F.E.)$$

$$\text{Pad Volume} = (\text{SLF Volume} \times \% \text{ Pad}) / (1 - \% \text{ Pad})$$

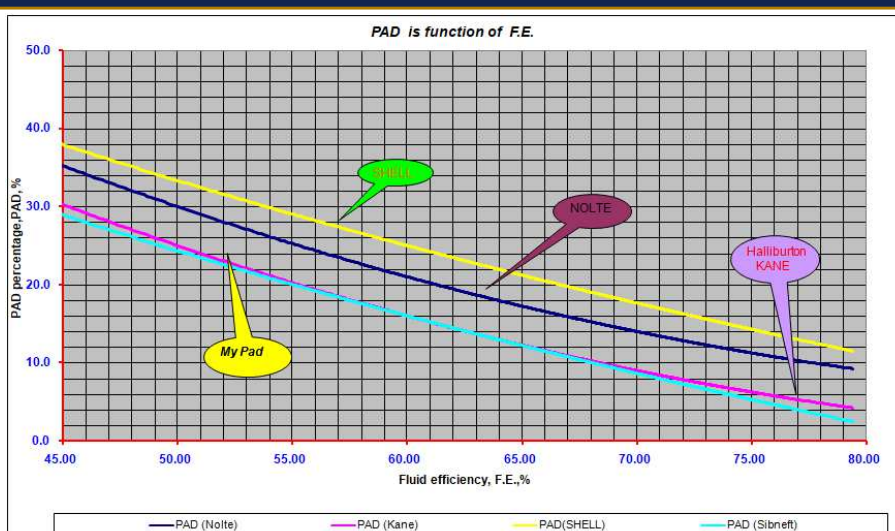
Nolte (1986)



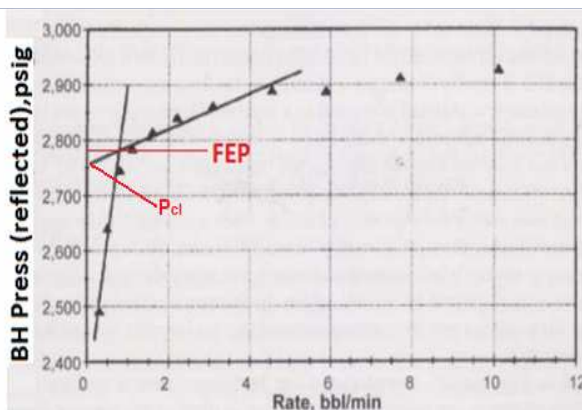
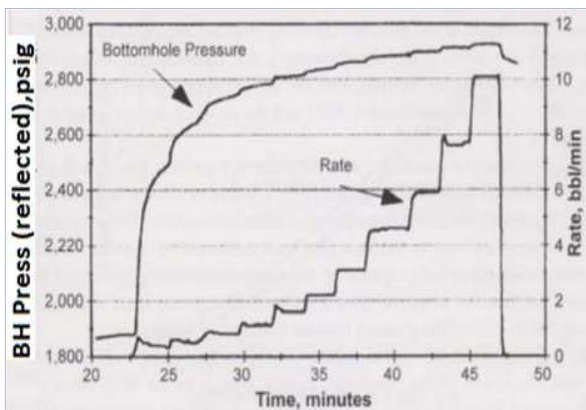
2.13 Pad vs. Fluid Efficiency (5-45%)



2.14 Pad vs. Fluid Efficiency (45-80%)



3.1.1 Step-up Rate Test (SRT)



FEP = Fracture Extension Pressure (upper bound for Pcl)

Tinker et al.(1997)

3.1.2 Step-up Rate Test



The SRT consists of two intervals: Injection (in steps up) and Shut-in.

■ **Theory:**

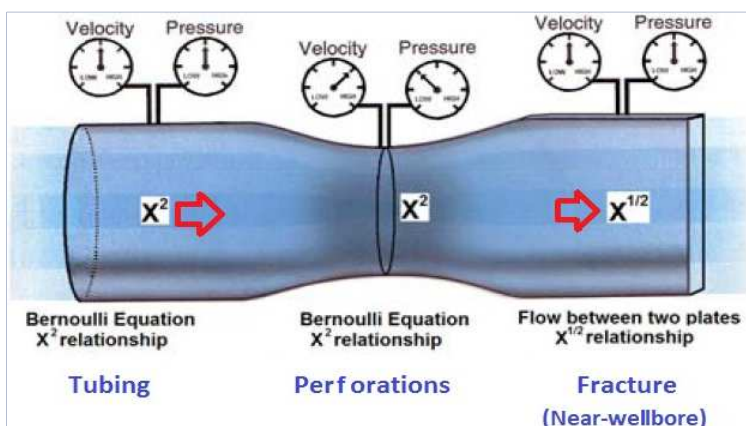
The only useful data obtained from the SRT is the **Fracture Extension Pressure (FEP)**, and **Closure Pressure Pcl**. FEP isn't very useful for **Conventional and Unconventional** Propped Hydraulic Fracturing. **FEP only serves as upper bound for Pcl**. Pcl can be determined by other methods.

■ **Procedure:**

1. Start the SRT by injecting at very low rate. Reason: Pressure increases dramatically at test initiation. Continue rate increase in slightly larger steps.
2. At about halfway through the test make the rate increases larger.
Reason: Small pressure increases are noted.
1. The last 3-4 rate increases should be very large.
Reason: Very small pressure increases are noted.



3.2.1 Well Friction Analogous to Venturi FM



Modified Venturi flow Meter (FM) represents well system.

- Upstream represents the Tubing
- Throat represents the Perforations

The flow rate for both is a X^2 relationship.

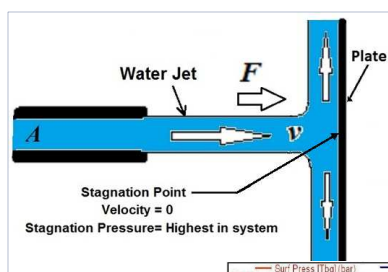
- Downstream represents the near wellbore area of the fracture. (parallel plate configuration)

The flow rate is a $X^{1/2}$ relationship.

Cleary et al. 1993
Massaras et al. 2007



3.2.2 Stagnation Pressure

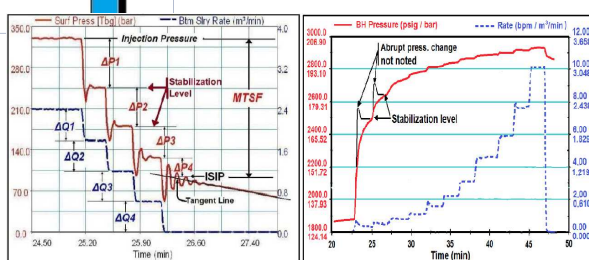


Only the Rate Step-down Test can be used for Friction Analysis.
RST cannot detect abrupt pressure changes

Jet impinging on a plate is analogous to jet flow via a perforation impinging at end of the perforation tunnel:

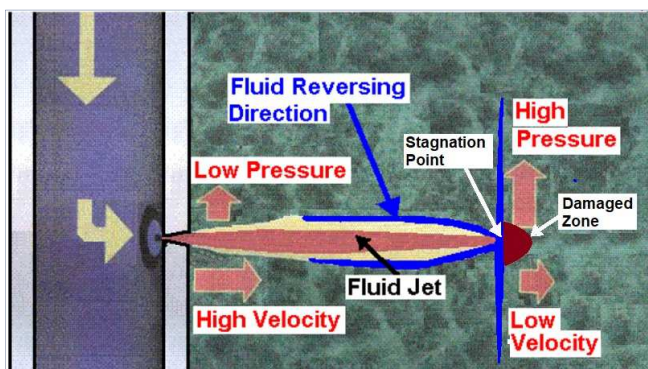
Because stagnation pressure is (at stagnation point) is very high, abrupt rate reductions during the RST result in instantaneous pressure reductions.

The opposite isn't true for the SRT.

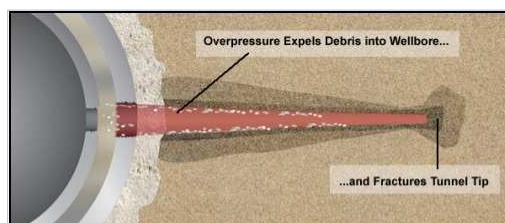


Massaras et al. 2011

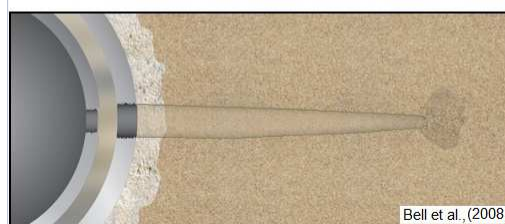
3.2.3 Perforation Friction



Perforation and fracture, showing the velocity and pressure relationships, a combination of which causes high stagnation pressure. [Massarar et al. (2007)]

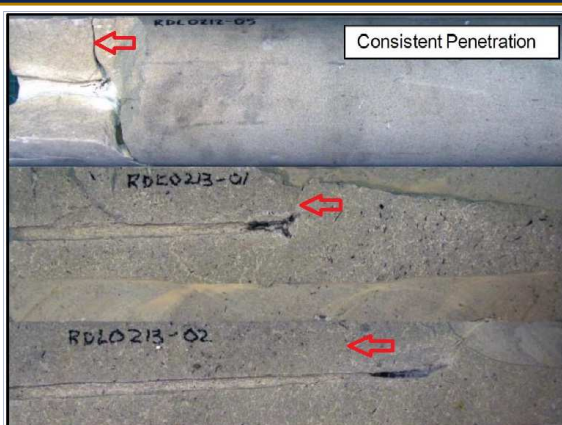


Over-pressure Expels Debris and Fractures Tip



New Debris-Free Tunnel with Fractured Tip [Bell et al., (2008)]

3.2.4 Perf Tip Damage



Consistent Penetration



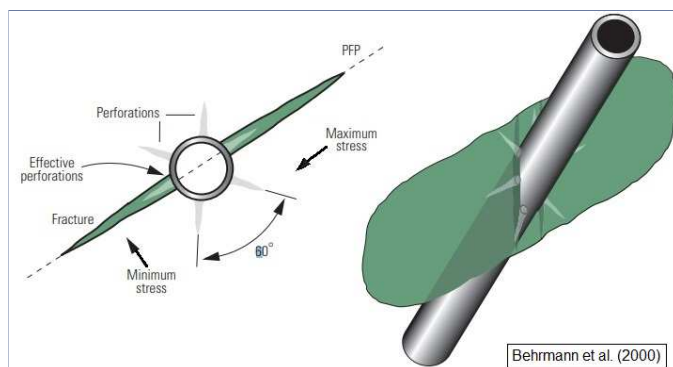
Comparison of consistent penetration charge against various similar conventional charges

[Cuthill et al. (2017)]



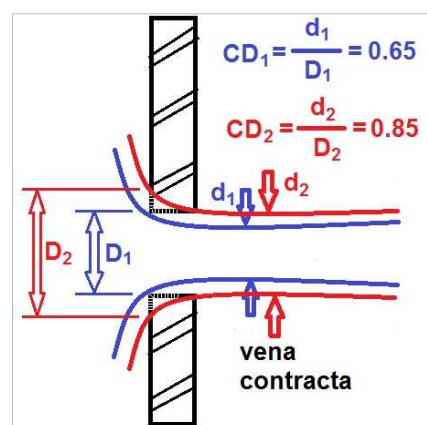
Flow is impinged similar to a bent garden hose, which **if bent enough** stops flow completely.

3.2.5 Effective Perforations



- Only 5% of wells are vertical at the perforated interval.
- 95% are inclined 1-5 deg.
- As such not all perforations are in contact with the fracture.
- Most wells are perforated with 6 SPF and 60 Φ.
- In a perforated interval of say 20 ft (120 perfs), probably only 5 ft are in contact with the fracture.
- Only 1/3 (2 perfs/ft) are **(effective)** accepting fluid.
- So max 5 ft x 2 perfs/ft = 10 perfs.
- Confirmed by solving for number of open perforations with the equations in next slide.

3.2.6 Very Few Perfs Open



Number of perforations accepting fluid can be calculated:

$$Q = \frac{D^2 C \sqrt{P}}{0.4967}$$

$$\text{Number of Perforations Open} = \frac{\text{Total Rate}}{Q}$$

D = Perforation diameter, in.

C = Coefficient

(0.65 before proppant, 0.95 after proppant)
(0.85 default in all simulators)

P = Pressure, psi

ρ = Density, lb/gal

The equations and coefficient (C), for perforation friction were developed with sharp corner perforations (drilled).

Example:

Perf. Diam. = 0.45 in

C = 0.65

P = 8000 psi

ρ = 8.33 lb/gal

Total Rate = 40 bpm

No. of Perfs Open = 4.9

3.2.7 RST Design Considerations



Incorporate the Rate Step (down) Test (RST) at end of Minifrac.

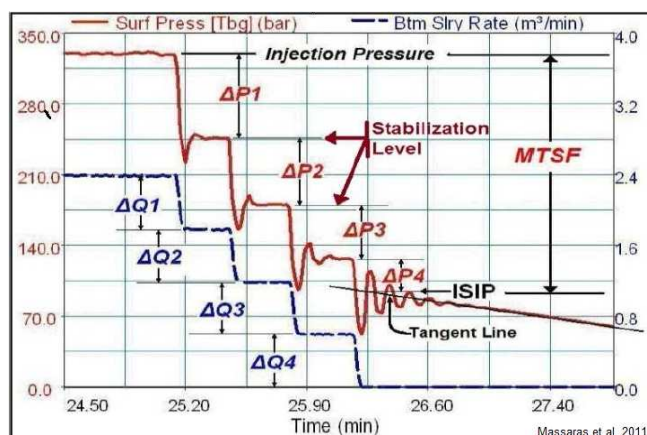
- **Make RST in 4 equal steps (or make 1st and 4th steps equal)**
 - Three steps is too few and five is too many.
 - Need enough data to:
 - See the plot curvature
 - See the expected progressive reduction in pressure trend (see next slide)
 - Obtain the Median Ratio (Massaras et al. (2012)).
- **Make steps very short (10-15 sec).**
- **Pump with 4 or 8 pumps all at about equal rate and take out 1 pump or 2 pumps at a time.**



3.2.8 RST Logic-ISIP Determination



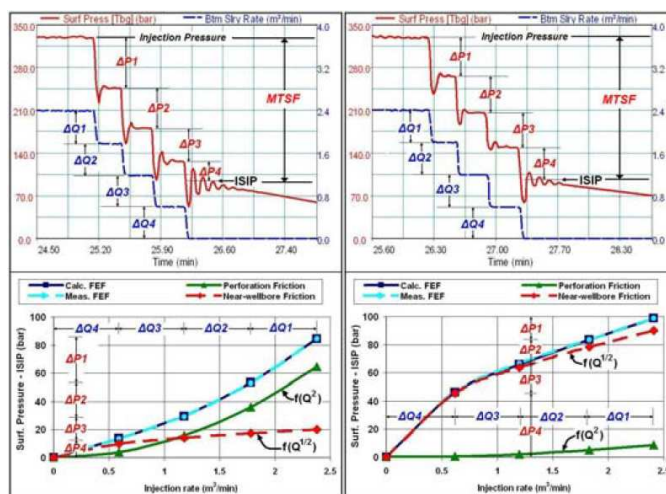
- Because most well parameters remain constant during short duration (30 -45 sec) of the RST, any deviation from the expected pattern of progressively smaller pressure reduction steps is a strong indication of hindrance to fluid flow.
- By the process of elimination, it can only be caused by a restrictive NWB area, and the associated NWB friction.



3.2.9 RST Differentiates FEF



- The RST differentiates Fracture Entry Friction into Perforation friction and near-wellbore friction (Tortuosity).
- If plot is concave upwards, perforation friction dominates (larger). If plot is concave sideways, near-wellbore friction dominates (larger).



Massaras et al 2007

3.2.10 FEF Guidelines



- Enhanced FEF Methodology has 45% success rate.
- Using also the Median Ratio increases the success rate to 90%.
- Each methodology is necessary but not sufficient for high rate of success.
- Indicators of high NWB Friction are:
 1. The Media Ratio (MR)= $\Delta P4/\Delta P1 \geq 0.5$
Massaras et al. (2011)
 2. Near-wellbore Friction ≥ 435 psi (30 bar)
Massaras et al. (2007)



General Decision Control Guideline
Based on Ranges of FEF Component Values

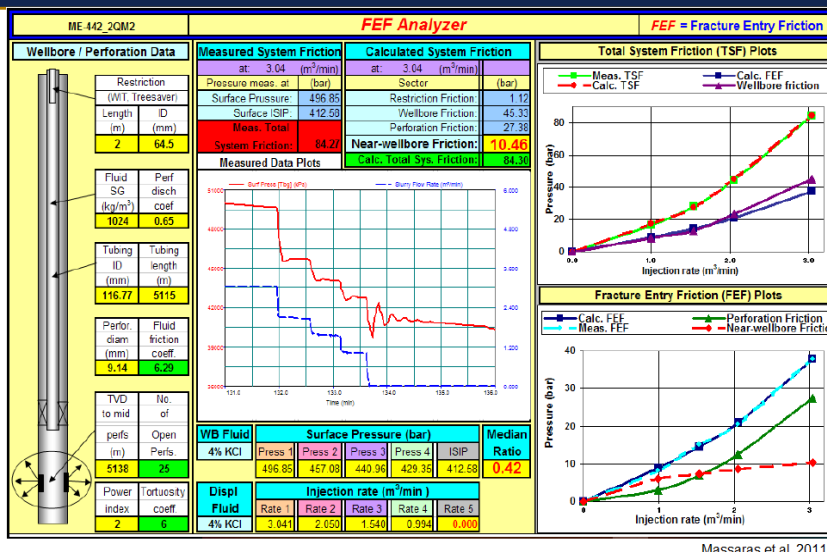
Perforation Friction		Near-wellbore Friction		Remarks
(bar)	(psi)	(bar)	(psi)	
0-15	0- 218	0 - 15	0- 218	Very low probability for screenout
15-30	218 - 435	15 -30	218- 435	Caution required
30-50	435-725	30-50	435-725	Screenout highly probable
> 50	> 725	> 50	> 725	Screenout almost certain

Massaras et al. (2007)

3.2.11 Low NWB Friction



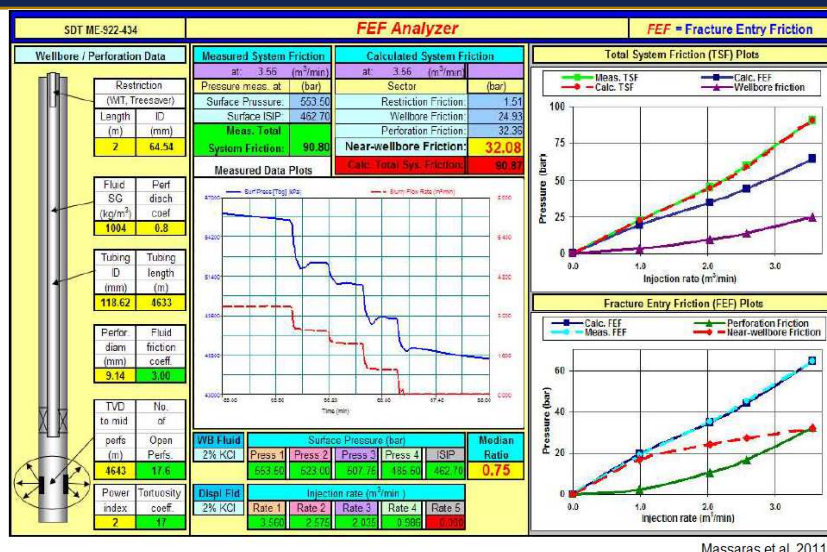
- DP4 small compared to DP1.
- Therefore NWB Friction low.
- NWB Friction 10.46 bar (< 30 bar)
- MR = 0.42



3.2.12 High NWB Friction



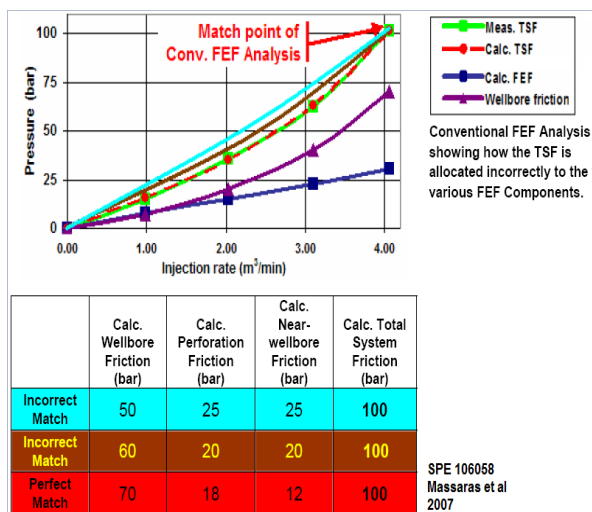
- DP4 large compared to DP1.
- Therefore NWB Friction high.
- NWB Friction 32.08 bar (> 30 bar)
- MR = 0.75



3.2.13 NWB Friction & Commercial Software



- Conventional FEF analysis has been implemented by most commercial Fracture Propagation Simulators.
- Matches TSF only at highest rate, this, causes misallocation of the friction into the three components. Cannot output unique solution.
- Enhanced FEF Analysis matches at all rates, thus, produces unique (correct) solution.



3.2.14 Frac Design from RST



- Data from RST used to design frac parameters:
 - Slope of prop ramp
 - Max prop concentration
 - Prop plateau duration
- Minifrac /DFIT and FEF Analysis are predictive.
- Real-time (RT) Monitoring and Analysis are required
- Monitor in RT: **Inverse Slope Method**. Massaras et al. (2012)



4.0 Before Closure Analysis (BCA) Methods



- Nolte (1979) and (1988)
- Barree and Mukherjee (1996)
- Barree et al. (2007) and (2009)

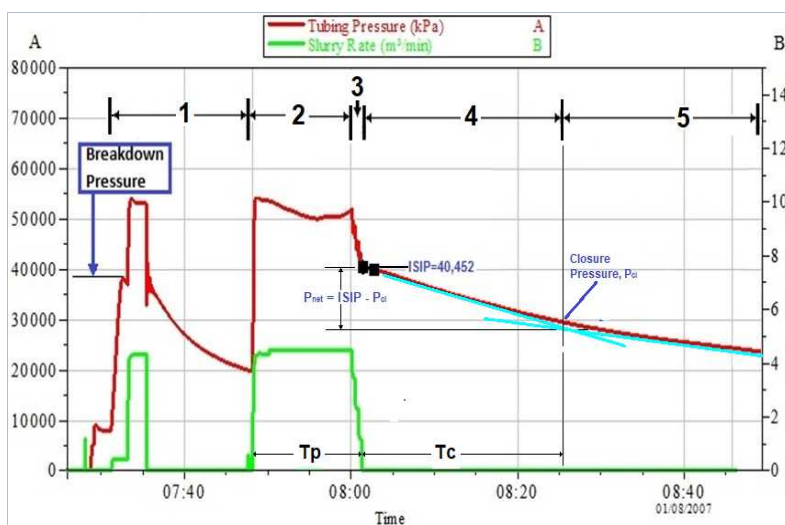


4.1 BCA Application



Before Closure Analysis, (BCA) is usually performed:

- On data from ISIP to fracture closure (interval 4).
- In real-time to ensure data is recorded until and past fracture closure.



4.2 Fracture and Reservoir Transient Flow Regimes

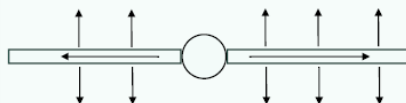


First step:
Determine Flow
Regime

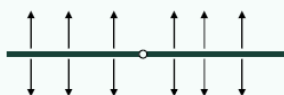
Fracture Linear Flow
(Tip-Extension, $\frac{1}{2}$ slope)



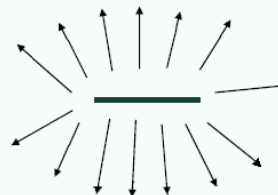
Bi-Linear Flow (Before closure, $\frac{1}{4}$ slope
After closure, $-\frac{3}{4}$ slope)



Formation Linear Flow
(Before closure, $\frac{1}{2}$ slope
After closure, $-\frac{1}{2}$ slope)



Pseudo-Radial Flow
(After closure, -1 slope)



Barree & Associates



4.3 BCA Analysis & Data



Before Closure Analysis

- Uses Special Derivatives and Time Functions:
 - **G-Function**
 - **Square-Root**
 - **Log-Log**
 - **Linear**
- Identifies Leakoff behavior, and Closure pressure

Data from Pre-Closure Analysis

- Fluid leak-off mechanisms
- Closure Pressure (P_{cl})
- Net pressure (P_{net})
- Min Horiz. Stress (σ_{min})
- Fluid/Fracture efficiency (E_f), (η)
- Flow regimes
- Reservoir pore pressure (P_r)
- Permeability (k)
- Fracture Length
- Leak-off Coefficient (C_L)

$$\eta = \frac{G_c}{2 + G_c}$$

$$C_L = \frac{2h}{\pi r_p E \sqrt{t_p}} \frac{dP}{dG}$$



4.4 G-Function Derivative analysis



- **G-Function Plots:**
 - Bottomhole pressure vs. G-Function
 - Derivative of pressure (dP/dG) vs. G-Function
 - Superposition derivative (GdP/dG) vs. G-Function
- **Characteristic shape of plots used to find:**
 - Detection of natural fractures
 - Leakoff type (Normal, PDL, Height Recession (or TS), Fracture Tip Extension)
 - Fluid Efficiency (η), $\eta = G_c / 2 + G_c$ (no spurt loss)



4.5 Algebraic Definition of G-Function



$G \approx 2v\Delta t_D$
for very
low perm
systems

G-function is a dimensionless function of shut-in time normalized to pumping time:

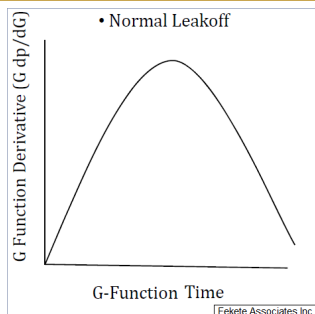
$$G(\Delta t_D) = \frac{4}{\pi} (g(\Delta t_D) - g_0)$$

$$\Delta t_D = (t - t_p) / t_p$$



Barree & Associates

4.6 G-Function: Two limiting cases



• Low Leakoff, high efficiency ($\alpha = 1.0$)

• Fracture area open varies approximately linear w/time

$$g(\Delta t_D) = \frac{4}{3} \left((1 + \Delta t_D)^{1.5} - \Delta t_D^{1.5} \right)$$

• High leakoff, low efficiency ($\alpha = 0.5$)

• Fracture area varies w/ square-root of time

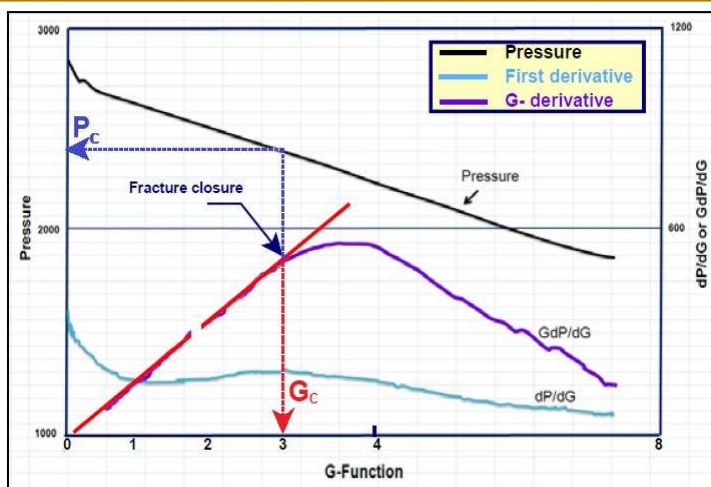
$$g(\Delta t_D) = (1 + \Delta t_D) \sin^{-1} \left((1 + \Delta t_D)^{-0.5} \right) + \Delta t_D^{0.5}$$

Barree & Associates

4.7 Normal (Ideal) Leakoff (NL)



- Fracture area constant during shut-in.
 - Leakoff through homogeneous matrix.
-
- Hump in First derivative (dP/dG)
 - G-Function derivative (GdP/dG) matches tangent that passes through origin.
 - Deviation of G-Function from tangent indicates Fracture Closure.

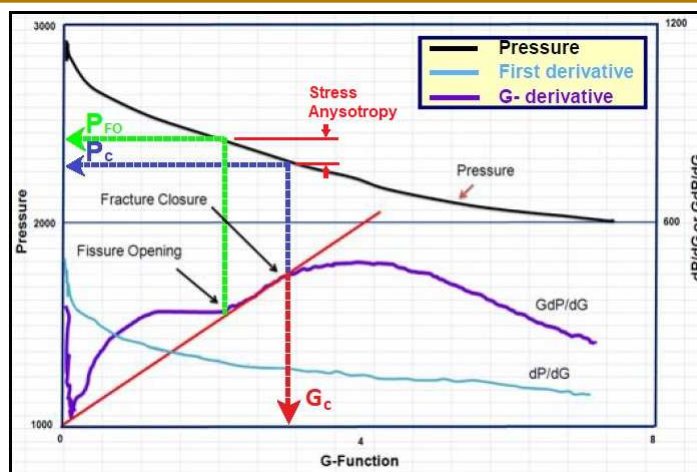


Adopted and Modified: Barree et al. (2007)

4-8 Pressure Dependent Leakoff (PDL)



- Indicates existence of secondary fractures in communication with the main fracture.
- G-Function derivative (GdP/dG)** exhibits large hump above the tangent line.
- Normal Leakoff after hump.
- End of hump indicates Fissure Opening.
- Deviation of **G-Function** from tangent indicates Fracture Closure.

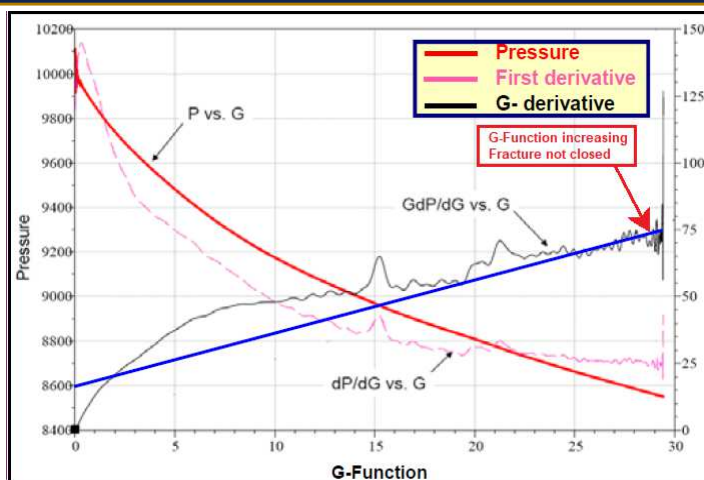


Adopted and Modified: Barree et al. (2007)

4.9 Fracture Tip Extension Leakoff (FTE)



- Fracture continues to grow after injection has stopped.
- Happens in very low permeability Reservoirs.
- Fluids which normally leakoff through adjacent zones, are transferred to the end of the fracture extending fracture at the tip.
- G-function derivative (GdP/dG)** initial has steep slope, which decreases with shut-in time, and yields concave-down curve.
- Tangent through the G-Function derivative ($G dP/dG$) intersects the y-axis above origin.



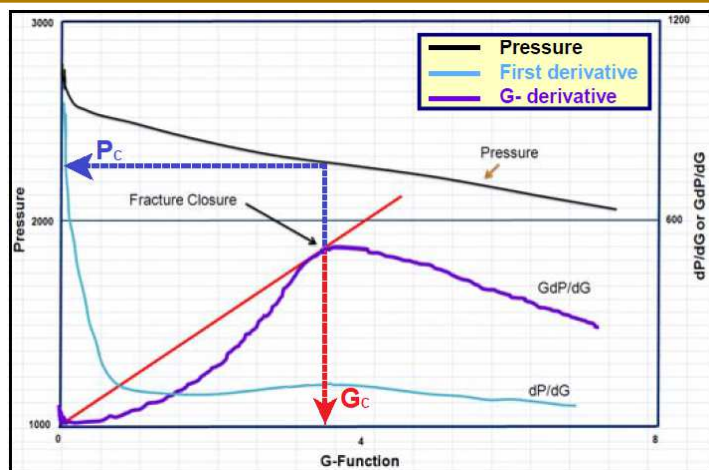
Adopted and Modified: Barree et al. (2007)

4.10 Height Recession Leakoff (HR)



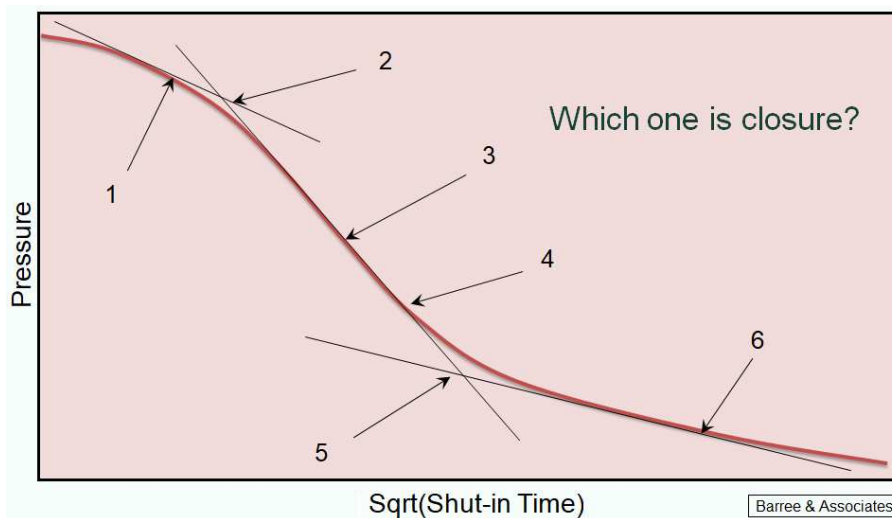
- Fracture grows into adjacent impermeable layers during injection.

- The G-Function derivative ($G \frac{dP}{dG}$) plots below the tangent line extrapolated through the normal leakoff data.
- Both G-Function and the first derivative exhibits a concave up trend.



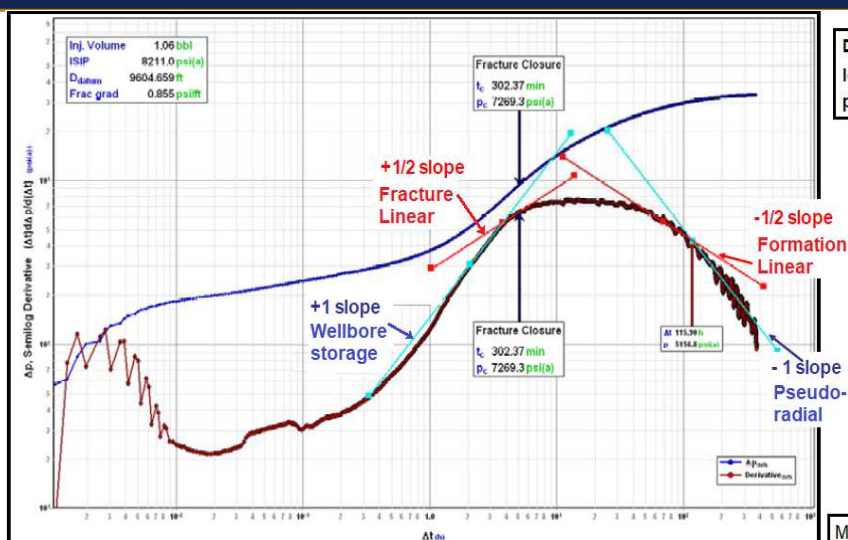
Adopted and Modified: Barree et al. (2007)

4.11 Square Root plot



Barree & Associates

4.12 Log-Log Plot



Diagnostic
log-log plot of
pressure falloff

Martin et al. (2012)

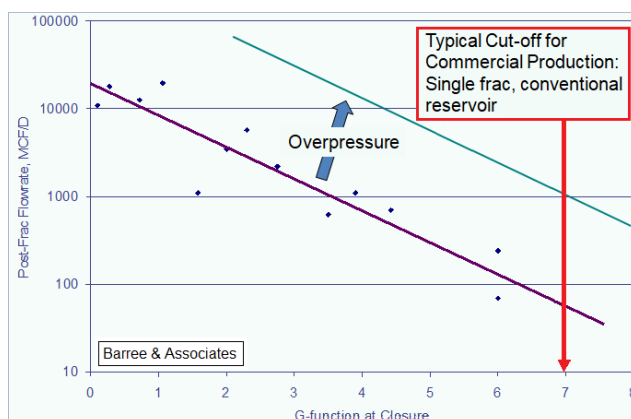
4.13 Log-Log Plot: Flow Regimes



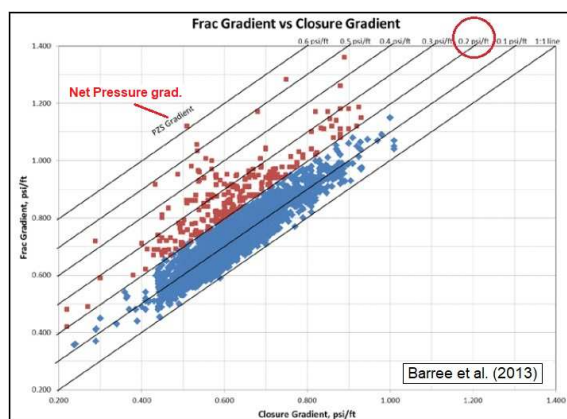
	Slope	Flow Pattern	Description
Before Closure	$\frac{1}{4}$	Bilinear	Fluid flows from the fracture along linear flow paths normal to the fracture and along the fracture.
	$\frac{1}{2}$	Fracture linear	Fluid flows along the fracture thus increasing fracture width.
After Closure	$-\frac{3}{4}$	Bilinear	Fluid flows from the fracture along linear flow paths normal to the fracture and along the fracture. (In reality, closure is unlikely to be truly instantaneous.)
	$-\frac{1}{2}$	Formation linear	Fluid flows into the formation in paths normal to the fracture plane.
	-1	Pseudo-radial	Fluid flows radially into the formation from the wellbore.



4.14 Commercial Production Cutoffs



G-Function time ≥ 7 - no flow



Pnet Gradient ≥ 0.2 psi/ft - no flow

5.1 ACA Techniques - Data



- Nolte (1997) based on Carslaw et al. (1959)
- Gu et al. (1993) based on Ayoub et al. (1988)
- Abousleiman et al. (1994)
- Soliman (2005) and (1986)
- Craig and Blasingame (2005)
- Mohamed et al. (2011)



- After Closure Analysis (ACA) has **similar** workflow to traditional **PTA**.
- Uses **"impulse"** solution to establish:
 - Formation permeability (k)
 - Reservoir pressure-Initial (P_i)
- Other Parameters
 - Flow Regime
 - Permeability (k)
 - Flow Capacity (kh)
 - Transmissibility (kh/μ)

5.2 Linear Flow Time Function (F_L)



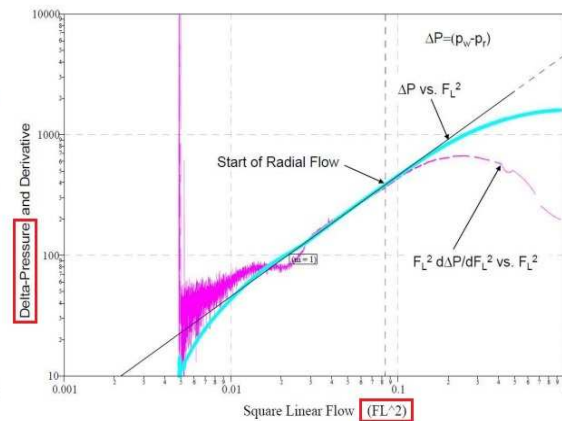
After closure analysis (ACA) is performed to identify the flow regime after closure takes place. The flow regimes can be described using characteristic slopes on a log-log plot of monitored pressure difference which is defined as fall-off pressure minus pore pressure versus the square of the linear flow time function (F_L^2).

The linear flow regime function (F_L) is described by Barree et al. (2007) as:

$$F_L(t, t_c) = \frac{2}{\pi} \sin^{-1} \sqrt{\frac{t_c}{t}} \quad \text{for } t \geq t_c \quad \text{and} \quad \Delta P = P - P_r$$

Pseudolinear flow, the slope of the derivative curve on the log-log plot should be 0.5

Pseudoradial flow, the slope of the derivative curve on the log-log plot should be 1 and the curves should coincide.



Barree et al. (2007)



5.3 Radial Flow Regime Function (F_R)



Cartesian plot of pressure versus F_R should yield a straight line with intercept equal to p_i and slope of m_R .

$$F_R(t, t_c) = \frac{1}{4} \ln \left(1 + \frac{\chi t_c}{t - t_c} \right), \quad \chi = \frac{16}{\pi^2} \cong 1.6$$

In the pseudoradial flow period the reservoir far-field transmissibility can be determined from the slope, fracture closure time, and volume injected.

$$\frac{kh}{\mu} = 251,000 \frac{Q_i}{m_R t_c}$$

k , permeability, md

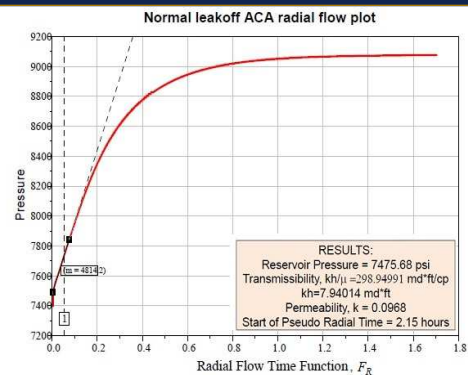
h , net pay thickness, feet

μ , far-field fluid viscosity, cp

t_c , fracture closure time, mins

Q_i , volume injected, bbls

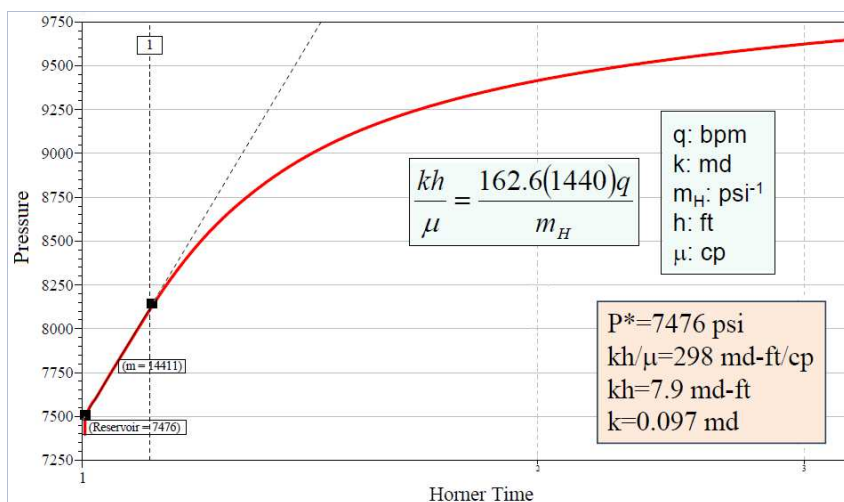
m_R , slope, psi



Barree et al. (2007)



5.4 Horner ACA



Only valid in
Pseudoradial flow

Barree et al. (2007)

5.5 Permeability – G-Function Time (Empirical)



Matrix permeability estimation with G-Function time

at closure (G_c):

$$k_m = \frac{0.0086 \mu_f \sqrt{0.01 P_{net}}}{\phi c_t (G_c E r_p / 0.038)^{1.96}}$$

where:

k_m = estimated matrix permeability,

P_{ISIP} = Instantaneous Shut-In Pressure (ISIP)

P_c = closure pressure

P_{net} = Net Pressure = $P_{ISIP} - P_c$

ϕ = porosity

E = Young's modulus

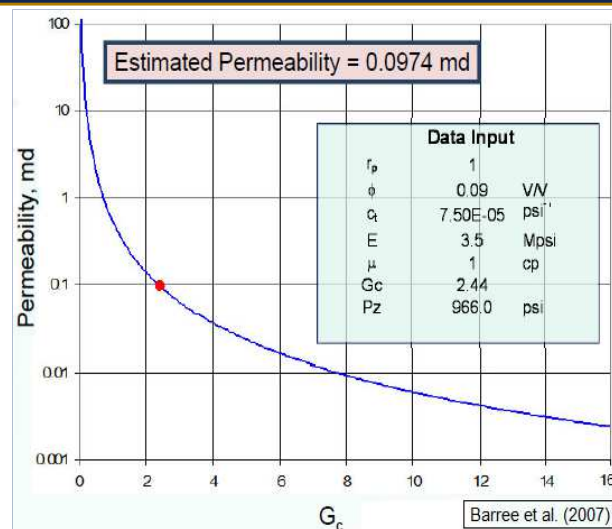
c_t = total compressibility

r_p = storage ratio

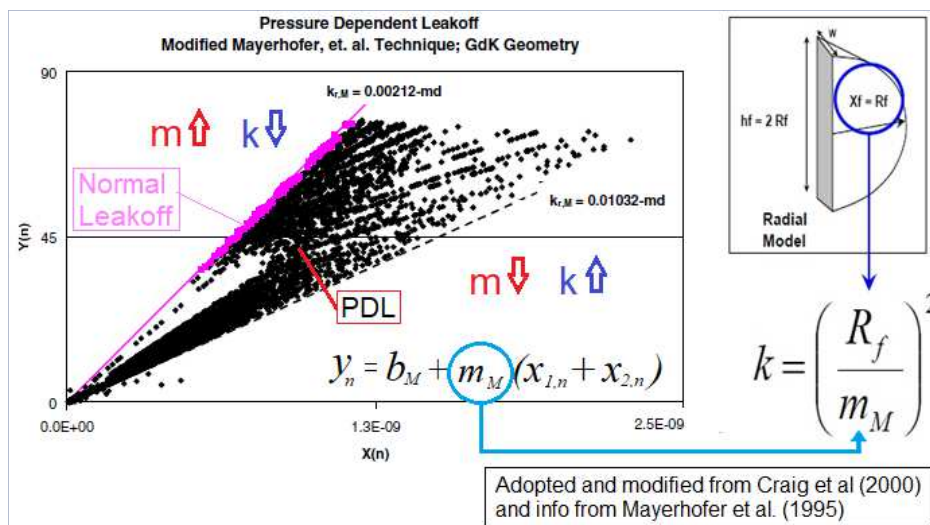
μ_f = fluid viscosity

G_c = G-time at closure

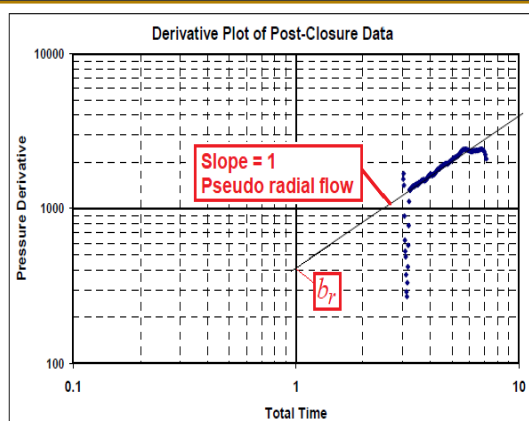
Barree et al. (2007)



5.6 Modified Mayerhofer: k



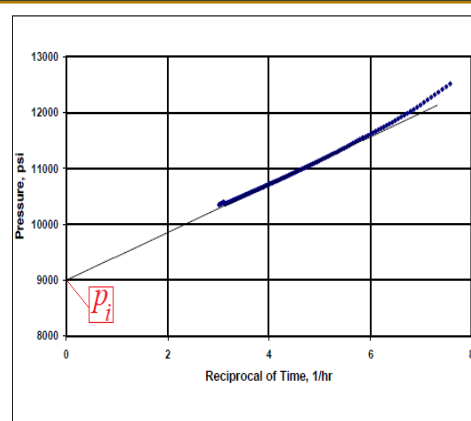
5.7 ACA Soliman-Craig: Radial - k and P_i



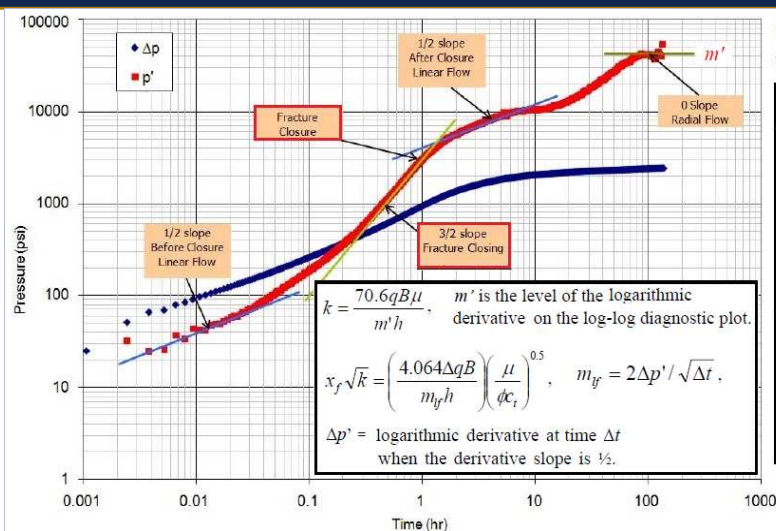
$$k = \frac{1694.4 V \mu}{b_r h}$$

V Injected volume bbl
 μ Viscosity, cp
 h Net pay thickness, ft
 b_r Intercept at time = 1
 p_i Initial reservoir pressure, psia

Modified from Soliman et al. (2005a)



5.8 Global Model for Minifrac Analysis



slope	
unit	Well-bore-storage
zero	Pseudo-radial flow
1/2	Linear flow
1/4	Bi-linear flow
-1/2	Spherical flow

Deviation of the derivative from the radial-flow straight-line indicates reservoir heterogeneities

Mohamed et al., (2011)

End & Questions



The End

Questions?



6.1 References



Introductory

Godbey, J. K., & Hodges, H. D. (1958, January 1). Pressure Measurements During Formation Fracturing Operations. Society of Petroleum Engineers.

Pump-in / Flowback

Savitski, A., & Dudley, J. W. (2011, January 1). Revisiting Microfrac In-situ Stress Measurement via Flow Back - A New Protocol. Society of Petroleum Engineers. doi:10.2118/**147248-MS**

Nolte, K. G. (1988, February 1). Application of Fracture Design Based on Pressure Analysis. Society of Petroleum Engineers. doi:10.2118/**13393-PA**

Plahn, S. V., Nolte, K. G., & Miska, S. (1995, January 1). A Quantitative Investigation of the Fracture Pump-In/Flowback Test. Society of Petroleum Engineers. doi:10.2118/**30504-MS**

Soliman, M. Y., & Daneshy, A. A. (1991, January 1). Determination of Fracture Volume and Closure Pressure From Pump-In/Flowback Tests. Society of Petroleum Engineers. doi:10.2118/**21400-MS**

Equilibrium Test

Poulsen, D. K. (1996, January 1). Equilibrium Minifracturing Test and Analysis. Society of Petroleum Engineers. doi:10.2118/**36438-MS**

Weng, X., Pandey, V., & Nolte, K. G. (2002, January 1). Equilibrium Test - A Method for Closure Pressure Determination. Society of Petroleum Engineers. doi:10.2118/**78173-MS**



6.2 References



Pump-in / Shut-in

Barree, R. D., Miskimins, J. L., & Gilbert, J. V. (2014, April 17). Diagnostic Fracture Injection Tests: Common Mistakes, Misfires, and Misdiagnoses. Society of Petroleum Engineers. doi:10.2118/**169539-MS**

Hawkes, R. V., Bachman, R., Nicholson, K., Cramer, D. D., & Chipperfield, S. T. (2018, October 16). Good Tests Cost Money, Bad Tests Cost More - A Critical Review of DFIT and Analysis Gone Wrong. Society of Petroleum Engineers. doi:10.2118/**191458-18IHFT-MS**

Rate Step-Down Test

Behrmann, L., et al., (2000) Perforating Practices That Optimize Productivity. Oilfield Review. Spring 2000:

Bell, M. R., & Cuthill, D. A. (2008, January 1). Next Generation Perforating System Enhances the Testing and Treatment of Fracture-Stimulated Wells in Canada. Society of Petroleum Engineers. doi:10.2118/**116226-MS**

Casero, A., Nicolaysen, A., Rylance, M., Clifton, J., & Fears, B. (2017, January 24). The Importance of Being Well Connected - High Rate Fracs in Horizontals. Society of Petroleum Engineers. doi:10.2118/**184813-MS**

Cipolla, C. L., Warpinski, N. R., Mayerhofer, M. J., Lolon, E., & Vincent, M. C. (2008, January 1). The Relationship Between Fracture Complexity, Reservoir Properties, and Fracture Treatment Design. Society of Petroleum Engineers. doi:10.2118/**115769-MS**

Cleary, M. P., Johnson, D. E., Kogsbøll, H.-H., Owens, K. A., Perry, K. F., de Pater, C. J., Mauro, T. (1993, January 1). Field Implementation of Proppant Slugs To Avoid Premature Screen-Out of Hydraulic Fractures With Adequate Proppant Concentration. Society of Petroleum Engineers. doi:10.2118/**25892-MS**

Cramer, D., Frieauf, K., Roberts, G., & Whittaker, J. (2019, January 29). Integrating DAS, Treatment Pressure Analysis and Video-Based Perforation Imaging to Evaluate Limited Entry Treatment Effectiveness. Society of Petroleum Engineers. doi:10.2118/**194334-MS**

Crump, J. B., & Conway, M. W. (1988, August 1). Effects of Perforation-Entry Friction on Bottomhole Treating Analysis. Society of Petroleum Engineers. doi:10.2118/**15474-PA**

Cuthill, D., Yang, W., & Hardesty, J. (2017, January 24). Improved Hydraulic Fracturing Perforation Efficiency Observed With Constant Entry Hole and Constant Penetration Perforating System. Society of Petroleum Engineers. doi:10.2118/**184878-MS**



6.3 References



- Keck, R. G., Reiter, D. F., Lynch, K. W., & Upchurch, E. R. (2000, January 1). Analysis of Measured Bottomhole Treating Pressures During Fracturing: Do Not Believe Those Calculated Bottomhole Pressures. Society of Petroleum Engineers. doi:10.2118/63033-MS
- Massaras, L. V., Dragomir, A., & Chiriac, D. (2007, January 1). Enhanced Fracture Entry Friction Analysis of the Rate Step-Down Test. Society of Petroleum Engineers. doi:10.2118/106058-MS
- Massaras, L. V., Massaras, D. V., & Al-Subhi, S. (2011, January 1). The Median Ratio and Near Wellbore Friction: Useful Proppant Admittance Criteria for Design and Placement of Safe and Effective Propped Hydraulic Fracture Treatments. Society of Petroleum Engineers. doi:10.2118/149092-MS

Pre- (Before) and Post- (After) Closure Analysis

- Abousleiman Y., et al., (1994) Formation Permeability Determination by Micro and Mini-Hydraulic Fracturing, June 1994, Journal of Energy Resources Technology, June 1994, ASME, Vol. 116 pp. 104-114, DOI: 10.1115/1.2906014
- Attanasi, E.D., Coburn, T.C. & Ran-McDonald, B. Nat Resour Res (2019) 28: 259. <https://doi.org/10.1007/s11053-018-9389-0>
- Ayoub, J. A., Bourdet, D. P., & Chauvel, Y. L. (1988, September 1). Impulse Testing. Society of Petroleum Engineers. doi:10.2118/15911-PA
- Bachman, R. C., Walters, D. A., Hawkes, R. A., Toussaint, F. L., & Settari, T. (2012, January 1). Reappraisal of the G Time Concept in Mini-Frac Analysis. Society of Petroleum Engineers. doi:10.2118/160169-MS
- Bachman, R., Afsahi, B., & Walters, D. (2015, June 9). Mini-Frac Analysis in Oilsands and their Associated Cap Rocks Using PTA Based Techniques. Society of Petroleum Engineers. doi:10.2118/174454-MS



6.4 References



- Craig, D. P., Eberhard, M. J., & Barree, R. D. (2000, January 1). Adapting High Permeability Leakoff Analysis to Low Permeability Sands for Estimating Reservoir Engineering Parameters. Society of Petroleum Engineers. doi:10.2118/60291-MS
- Barree, R. D., & Mukherjee, H. (1996, January 1). Determination of Pressure Dependent Leakoff and Its Effect on Fracture Geometry. Society of Petroleum Engineers. doi:10.2118/36424-MS
- Barree, R. D. (1998, January 1). Applications of Pre-Frac Injection/Falloff Tests in fissured Reservoirs - Field Examples. Society of Petroleum Engineers. doi:10.2118/39932-MS
- Barree, R. D., Barree, V. L., & Craig, D. (2007, January 1). Holistic Fracture Diagnostics. Society of Petroleum Engineers. doi:10.2118/107877-MS
- Barree, R. D., Barree, V. L., & Craig, D. (2009, August 1). Holistic Fracture Diagnostics: Consistent Interpretation of Prefrac Injection Tests Using Multiple Analysis Methods. Society of Petroleum Engineers. doi:10.2118/107877-PA
- Barree, R. D., Harris, H. G., Towler, B. F., & Ramurthy, M. (2013, November 11). Effects of High Pressure-Dependent Leakoff (PDL) and High Process-Zone Stress (PZS) on Stimulation Treatments and Production. Society of Petroleum Engineers. doi:10.2118/167038-MS
- Barree, R. D., Miskimins, J. L., & Gilbert, J. V. (2014, April 17). Diagnostic Fracture Injection Tests: Common Mistakes, Misfires, and Misdiagnoses. Society of Petroleum Engineers. doi:10.2118/169539-MS
- Benekadi, S., & Tiab, D. (2001, January 1). Reservoir Permeability Determination Using After-Closure Period Analysis of Calibration Tests. Society of Petroleum Engineers. doi:10.2118/70062-MS
- Benekadi, S., Belhaouas, R., & Sahar, M. (2003, January 1). Use of After Closure Analysis to Improve Hydraulic Fracturing Designs, Application on Algeria's In-Adaoui gas Field. Society of Petroleum Engineers. doi:10.2118/80936-MS
- Bourdet, D., & Gringarten, A. C. (1980, January 1). Determination Of Fissure Volume And Block Size In Fractured Reservoirs By Type-Curve Analysis. Society of Petroleum Engineers. doi:10.2118/9293-MS
- Bourdet, D., Ayoub, J. A., & Pirard, Y. M. (1989, June 1). Use of Pressure Derivative in Well Test Interpretation. Society of Petroleum Engineers. doi:10.2118/12777-PA



6.5 References



- Carslaw, H.S. and Jaeger, J.C.: "Conduction of Heat in Solids". Oxford University Press, 2nd Ed. P 76, 1959.
- Ceccarelli, R. L., Ciuca, A., & Tambini, M. (2009, January 1). New Methodology of Mini-Fall-Off Test to Optimize Hydraulic Fracturing in Unconventional Reservoirs. Society of Petroleum Engineers. doi:10.2118/122326-MS
- Cinco L., H., Samaniego V., F., & Dominguez A., N. (1978, August 1). Transient Pressure Behavior for a Well With a Finite-Conductivity Vertical Fracture. Society of Petroleum Engineers. doi:10.2118/6014-PA
- Craig, D. P., Eberhard, M. J., & Barree, R. D. (2000, January 1). Adapting High Permeability Leakoff Analysis to Low Permeability Sands for Estimating Reservoir Engineering Parameters. Society of Petroleum Engineers. doi:10.2118/60291-MS
- Craig, D. P., & Blasingame, T. A. (2006, January 1). Application of a New Fracture-Injection/Falloff Model Accounting for Propagating, Dilated, and Closing Hydraulic Fractures. Society of Petroleum Engineers. doi:10.2118/100578-MS
- Craig, D. P. (2014, April 1). New Type Curve Analysis Removes Limitations of Conventional After-Closure Analysis of DFIT Data. Society of Petroleum Engineers. doi:10.2118/168988-MS
- Ewens, S. D., Idorenyin, E. H., Donnell, P., Brunner, F., & Santo, M. (2012, January 1). Executing Minifrac Tests and Interpreting After-Closure Data for Determining Reservoir Characteristics in Unconventional Reservoirs. Society of Petroleum Engineers. doi:10.2118/162779-MS
- Gu, H., Elbel, J. L., Nolte, K. G., Cheng, A. -D., & Abousleiman, Y. (1993, January 1). Formation Permeability Determination Using Impulse-Fracture Injection. Society of Petroleum Engineers. doi:10.2118/25425-MS
- Gulrajani, S.N., Nolte, K.G., (2000) "Fracture Evaluation Using Pressure Diagnostics", in *Reservoir Stimulation* 3rd Edition, Eds Economides, M.J., Nolte, K.G., Wiley Publishers. ISBN-10: 0471491926, ISBN-13: 978-0471491927



6.6 References



- Hawkes, R. V., Bachman, R., Nicholson, K., Cramer, D. D., & Chipperfield, S. T. (2018, October 16). Good Tests Cost Money, Bad Tests Cost More – A Critical Review of DFIT and Analysis Gone Wrong. Society of Petroleum Engineers. doi:10.2118/191458-18IHFT-MS
- HIS Markit (2019) Webinar: Case Study: Improve Your RTA Results - Integrate PTA for Reduced Uncertainty
- Jones, J. R., Britt, L. K., (2009) "Design and Appraisal of Hydraulic Fractures", Society of Petroleum Engineers, Richardson, TX, USA, ISBN: 978-1-55563-143-7.
- Kazemi, M., & Takbiri-Borujeni, A. (2015, September 28). Predicting Gas Apparent Permeability of Shale Samples: A Novel Analytical Approach. Society of Petroleum Engineers. doi:10.2118/175035-MS
- Martin, R., Cramer, D. D., Nunez, O., & Roberts, N. R. (2012, January 1). A Method To Perform Multiple Diagnostic Fracture Injection Tests Simultaneously in a Single Wellbore. Society of Petroleum Engineers. doi:10.2118/152019-MS
- Mayerhofer, M. J., Ehlig-Economides, C. A., & Economides, M. J. (1995, March 1). Pressure Transient Analysis of Fracture Calibration Tests. Society of Petroleum Engineers. doi:10.2118/26527-PA
- Mohamed, I. M., Azmy, R. M., Sayed, M. A. I., Marongiu-Porcu, M., & Economides, C. (2011, January 1). Evaluation of After-Closure Analysis Techniques for Tight and Shale Gas Formations. Society of Petroleum Engineers. doi:10.2118/140136-MS
- Naidu, R. N., Guevara, E. A., Twynam, A. J., Rueda, J. I., Dawson, W., Moses, E., & Rylance, M. (2015, January 26). Understanding Unusual Diagnostic Fracture Injection Test Results In Tight Gas Fields - A Holistic Approach To Resolving The Data. Society of Petroleum Engineers. doi:10.2118/172956-MS
- Nolte, K. G., & Smith, M. B. (1979, January 1). Interpretation of Fracturing Pressures. Society of Petroleum Engineers. doi:10.2118/8297-MS
- Nolte, K. G. (1982, January 1). Fracture Design Considerations Based on Pressure Analysis. Society of Petroleum Engineers. doi:10.2118/10911-MS
- Nolte, K. G. (1986, July 1). Determination of Proppant and Fluid Schedules From Fracturing-Pressure Decline. Society of Petroleum Engineers. doi:10.2118/13278-PA
- Nolte, K. G., Maniere, J. L., & Owens, K. A. (1997, January 1). After-Closure Analysis of Fracture Calibration Tests. Society of Petroleum Engineers. doi:10.2118/38676-MS



6.7 References



- Nolte, K. G. (1997, January 1). Background for After-Closure Analysis of Fracture Calibration Tests. Society of Petroleum Engineers. SPE-39407-MS.
- Soliman, M. Y. (1986, August 1). Analysis of Buildup Tests With Short Producing Time. Society of Petroleum Engineers. doi:10.2118/11083-PA
- Soliman, M. Y., Azari, M., Ansah, J., & Kabir, C. S. (2004, January 1). Design, Interpretation, and Assessment of Short-Term Pressure-Transient Tests. Society of Petroleum Engineers. doi:10.2118/90837-MS
- Soliman, M. Y., Craig, D. P., Bartko, K. M., Rahim, Z., & Adams, D. M. (2005a, January 1). Post-Closure Analysis to Determine Formation Permeability, Reservoir Pressure, Residual Fracture Properties. Society of Petroleum Engineers. doi:10.2118/93419-MS
- Soliman, M. Y., Azari, M., Ansah, J., & Kabir, C. S. (2005b, January 1). Review and Application of Short-Term Pressure Transient Testing of Wells. Society of Petroleum Engineers. doi:10.2118/93560-MS
- Soliman, M. Y., Craig, D., Bartko, K., Rahim, Z., Ansah, J., Adams, D., (2005c, January 1). ARMA/USRMS 05-658. New Method for Determination of Formation Permeability, Reservoir Pressure, and Fracture Properties from a Minifrac Test. *American Rock Mechanics Association*.
- Soliman, M. Y., Miranda, C. G., & Wang, H. (2009, January 1). After Closure Analysis for Unconventional Reservoirs and Completion. Society of Petroleum Engineers. doi:10.2118/124135-MS
- Soliman, M. Y., Miranda, C., & Wang, H. M. (2010a). Application of After-Closure Analysis to a Dual-Porosity Formation, to CBM, and to a Fractured Horizontal Well. *SPE Production & Operations*, 25(04), 472–483. doi:10.2118/124135-PA
- Soliman, M. Y., Thornton, K. V., Miranda, C. G., & Wang, H. (2010b, January 1). Investigation of Effect of Fracturing Fluid on After-Closure Analysis in Gas Reservoirs. Society of Petroleum Engineers. doi:10.2118/128016-MS
- Talley, G. R., Swindell, T. M., Waters, G. A., & Nolte, K. G. (1999, January 1). Field Application of After-Closure Analysis of Fracture Calibration Tests. Society of Petroleum Engineers. doi:10.2118/52220-MS



6.8 References



- Valko, P., & Economides, M. J. (1997, January 1). Fluid Leakoff Delineation in High-Permeability Fracturing. Society of Petroleum Engineers. doi:10.2118/37403-MS
- Valko, P., & Economides, M. J. (1995), *Hydraulic Fracture Mechanics*, Wiley, Chichester.
- Wang, H., & Sharma, M. M. (2018, January 23). Estimating Unproped Fracture Conductivity and Compliance from Diagnostic Fracture Injection Tests. Society of Petroleum Engineers. doi:10.2118/189844-MS
- Xue, H., & Ehlig-Economides, C. (2013, August 12). Permeability Estimation from Fracture Calibration Test Analysis in Shale and Tight Gas. Unconventional Resources Technology Conference. doi:10.15530/URTEC-1569587-MS

Type Curve Analysis

- Craig, D.P. and Blasingame, T.A. 2006. Application of a New Fracture-Injection/Falloff Model Accounting for Propagating, Dilated, and Closing Hydraulic Fractures. <https://doi.org/10.2118/100578-MS>
- Craig, D.P. 2014. New Type Curve Analysis Removes Limitations of Conventional After-Closure of DFIT Data. <https://doi.org/10.2118/168988-MS>
- Craig, D.P. & Jackson, R.A. 2017 Calculating the Volume-of-Reservoir Investigated During a Fracture-Injection/Falloff Test DFIT. <https://doi.org/10.2118/184820-MS>

